

EMP : 1. PISNI IZPIT

$$\boxed{1} + \left\{ \begin{array}{l} \mu_{mm1} = NI_1 S \\ \vec{B} = \frac{\mu_0}{4\pi} \frac{3(\vec{r}_{mm} \cdot \vec{r}) \vec{r} - r^2 \vec{r}_{mm}}{r^5} \end{array} \right\} +$$

$$B_2 = -\frac{\mu_0}{4\pi} \frac{\mu_{mm1}}{r^3} \quad \leftarrow \quad \vec{B} (\vec{r} \perp \vec{r}_{mm}) = -\frac{\mu_0}{4\pi} \frac{\vec{r}_{mm}}{r^3} \quad \left. \right\} +$$

$$+ \left\{ \Phi_2 = NB_2 S = -\underbrace{\frac{\mu_0}{4\pi} \frac{N^2 S^2}}_{L_{21}} I_1 \right.$$

$$\frac{1}{4} \left\{ \begin{array}{l} U_2 = -\dot{\Phi}_2 = -L_{21} \dot{I}_1 = -L_{21} \omega I_1, \quad U_2 = L_2 \dot{I}_2 = L_2 \omega I_2 \end{array} \right.$$

$$\frac{1}{4} \left\{ \frac{I_2}{I_1} = -\frac{L_{21}}{L_2} = \frac{\frac{\mu_0}{4\pi} \frac{N^2 S^2}{r^3}}{\frac{\mu_0 N^2 S}{l}} = \frac{1}{4\pi} \frac{Sl}{r^3} = \boxed{\frac{V}{4\pi r^3}} \quad \boxed{1}$$

$$\boxed{2} + \left\{ \begin{array}{l} U(r) = \begin{cases} A r \cos \vartheta & , r < a \\ \frac{B}{r^2} \cos \vartheta - E_0 r \cos \vartheta & , r > a \end{cases} \end{array} \right.$$

$$\frac{1}{4} \left\{ \begin{array}{l} \text{RP1) } U(a^-) = U(a^+) \Rightarrow A = \frac{B}{a^3} - E_0 \\ \text{RP2) } \epsilon E_{\perp}(a^-) = E_{\perp}(a^+) \Rightarrow \epsilon A = -\frac{2B}{a^3} - E_0 \end{array} \right\} \Rightarrow \begin{array}{l} A = -\frac{3}{\epsilon+2} E_0 \\ B = \frac{\epsilon-1}{\epsilon+2} a^3 E_0 \end{array}$$

$$+ \left\{ \begin{array}{l} \sigma_r = \epsilon_0 [E(a^+) - E(a^-)] = \epsilon_0 \left(\frac{2B}{a^3} + E_0 + A \right) \cos \vartheta \\ \sigma_r = \epsilon_0 \frac{3(\epsilon-1)}{\epsilon+2} E_0 \cos \vartheta \end{array} \right.$$

$$\frac{1}{4} \left\{ \begin{array}{l} dS = 2\pi a^2 d(\cos \vartheta) \\ \epsilon r = \int \sigma_r dS = \epsilon_0 \frac{3(\epsilon-1)}{\epsilon+2} E_0 \cdot 2\pi a^2 \int_{\cos \vartheta = 0}^1 \cos \vartheta d(\cos \vartheta) = \boxed{\frac{3(\epsilon-1)}{\epsilon+2} \epsilon_0 E_0 \pi a^2} \end{array} \right.$$

$$\frac{1}{4} \left\{ \begin{array}{l} U(r > a) = \frac{\epsilon_0 4\pi B \cos \vartheta}{4\pi \epsilon_0 r^2} - E_0 r \cos \vartheta \\ \frac{\mu_r \cos \vartheta}{4\pi \epsilon_0 r^2} \Rightarrow \mu_r = 4\pi \epsilon_0 B = \boxed{\frac{\epsilon-1}{\epsilon+2} 4\pi \epsilon_0 a^3 E_0} \end{array} \right. \quad \boxed{1}$$

3

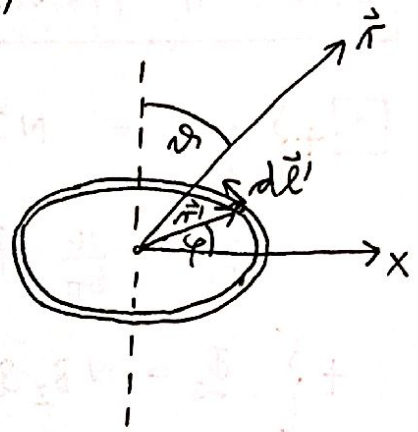
$$\vec{B} = -\frac{\mu_0}{4\pi\epsilon_0 r} \hat{e}_r \times \int \frac{\partial}{\partial t} \vec{j}(\vec{r}', t_r + \frac{\vec{r} \cdot \vec{r}'}{rc_0}) d^3 r'$$

$$\vec{j} d^3 r' = I d\vec{l}'$$

$$I = I_0 \sin \omega t$$

$$\vec{r} = r \begin{bmatrix} \sin \vartheta \\ \vartheta \\ \cos \vartheta \end{bmatrix}$$

$$\vec{r}' = a \begin{bmatrix} \cos \varphi \\ \sin \varphi \\ \vartheta \end{bmatrix} \Rightarrow d\vec{l}' = a d\varphi \begin{bmatrix} -\sin \varphi \\ \cos \varphi \\ \vartheta \end{bmatrix}$$



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$$\frac{\vec{r} \cdot \vec{r}'}{rc_0} = \frac{a}{c_0} \cos \varphi \sin \vartheta \Rightarrow \vec{j} d^3 r' = a I_0 \sin(\omega t_r + \frac{\omega a}{c_0} \cos \varphi \sin \vartheta) \begin{bmatrix} -\sin \varphi \\ \cos \varphi \\ \vartheta \end{bmatrix} d\varphi$$

$$\frac{\partial}{\partial t} \vec{j} d^3 r' = a I_0 \omega \cos(\omega t_r + \frac{\omega a}{c_0} \cos \varphi \sin \vartheta) \begin{bmatrix} -\sin \varphi \\ \cos \varphi \\ \vartheta \end{bmatrix} d\varphi$$

$$\cos \omega t_r \cos(\frac{\omega a}{c_0} \sin \vartheta \cdot \cos \varphi) - \sin \omega t_r \sin(\frac{\omega a}{c_0} \sin \vartheta \cdot \cos \varphi)$$

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$$\int_0^{2\pi} \frac{\partial}{\partial t} \vec{j} d^3 r' \rightarrow \text{prezivile} \int_0^{2\pi} \cos \varphi \sin(\frac{\omega a}{c_0} \sin \vartheta \cdot \cos \varphi) d\varphi = 2\pi J_1(\frac{\omega a}{c_0} \sin \vartheta)$$

+

$$\vec{B} = -\frac{\mu_0}{4\pi\epsilon_0 r} a I_0 \omega (-\sin \omega t_r) \underbrace{\hat{e}_r \times \hat{e}_\varphi}_{-\hat{e}_\vartheta} 2\pi J_1(\frac{\omega a}{c_0} \sin \vartheta)$$

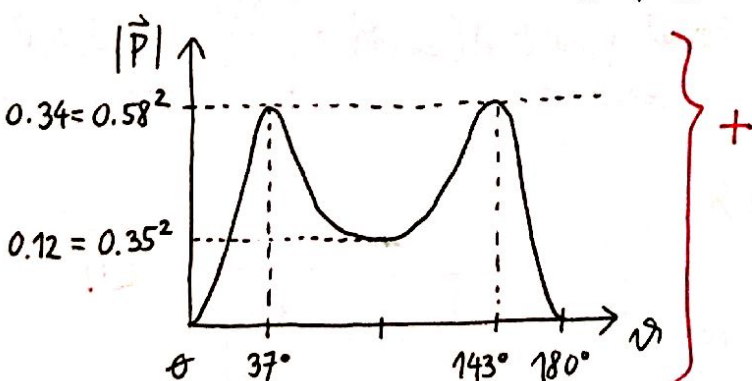
$$\vec{B} = -\frac{\mu_0 I_0}{2\pi} \frac{\omega a}{c_0} \sin \omega t_r \hat{e}_\vartheta J_1(\frac{\omega a}{c_0} \sin \vartheta), \quad 2\pi a = 3\lambda$$

$$\frac{\omega a}{c_0} = a \frac{2\pi}{\lambda} = a \frac{3}{a} = 3$$

$$|\vec{P}| \propto B^2 \propto J_1^2(3 \sin \vartheta)$$

$\in [-3, 3] \Rightarrow$ en maksimum med ϑ & $\frac{\pi}{2}$

graf: $3 \sin \vartheta \approx 1.8 \Rightarrow \vartheta \approx 37^\circ$
 $\vartheta \approx 143^\circ$



Vprašanje glede primerjave
 iz MAJHNO ravnice je slabo formulirano.